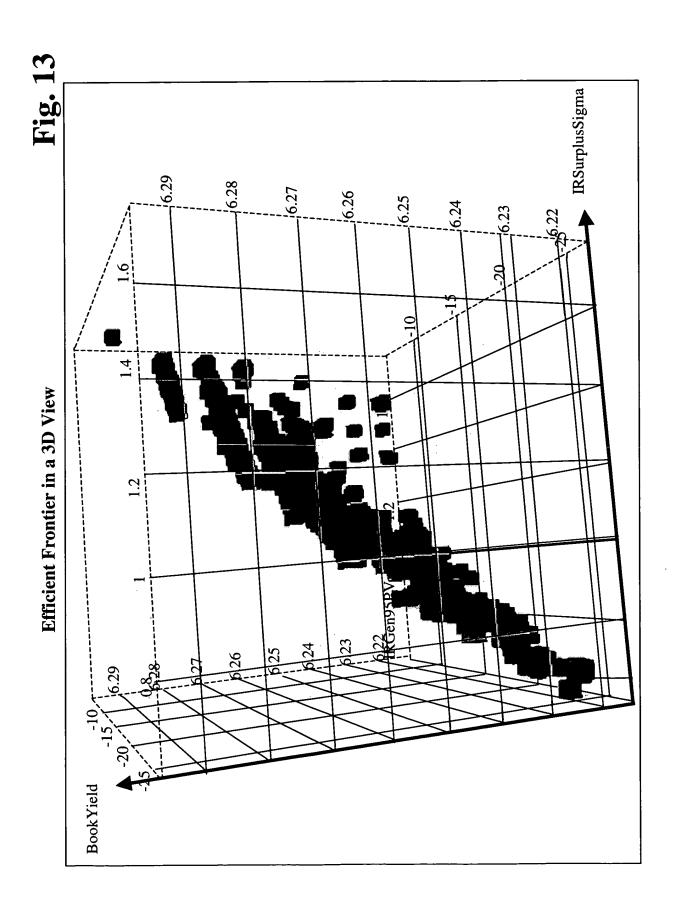
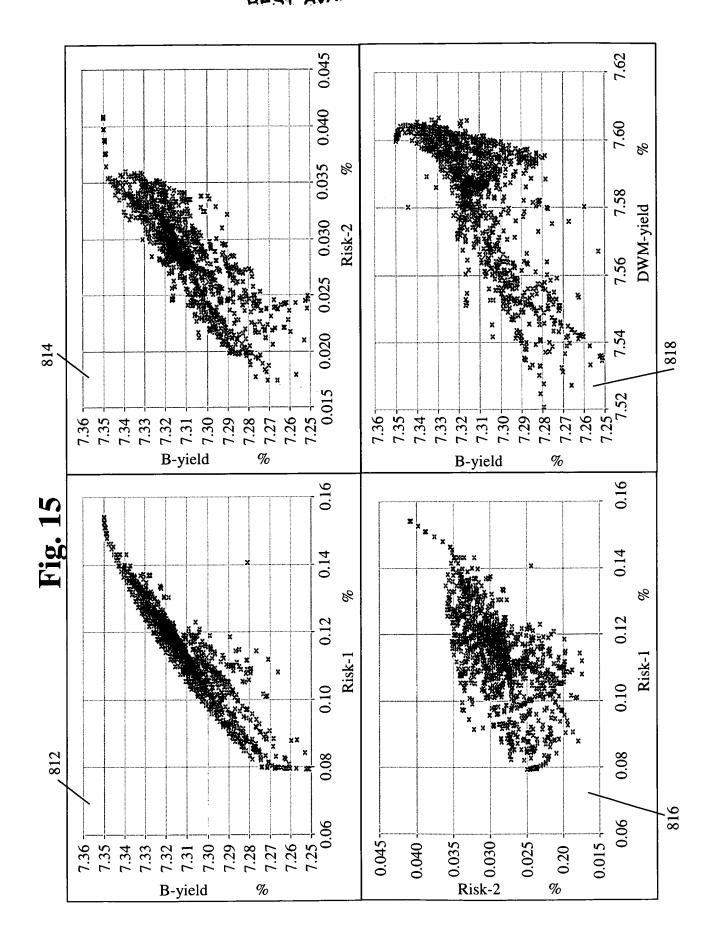


Process to interactively fill any gaps in the identified efficient frontier

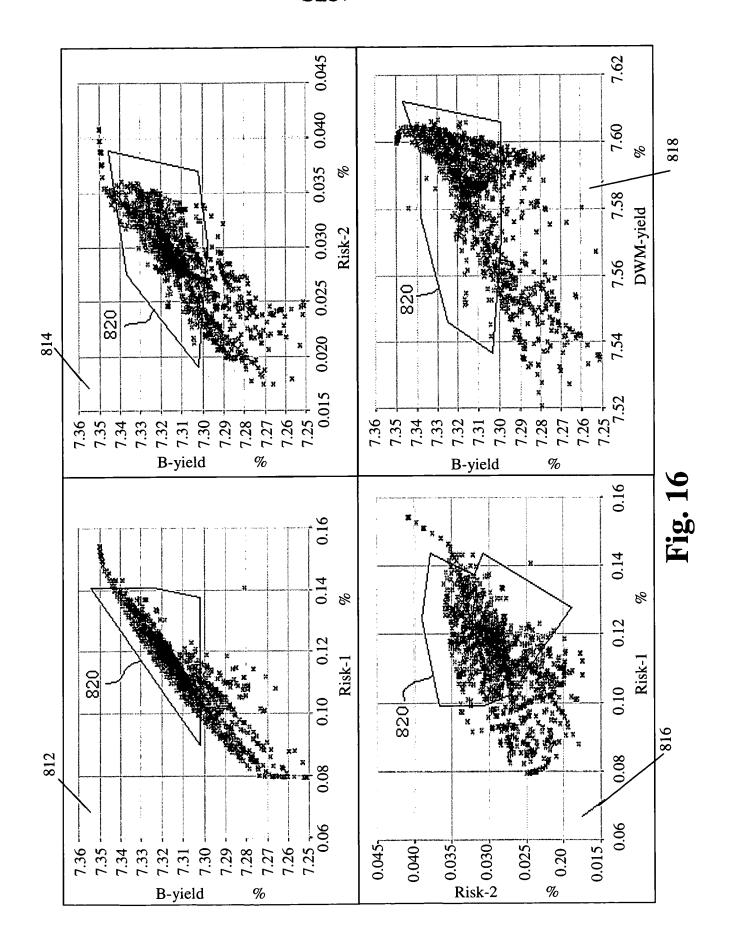


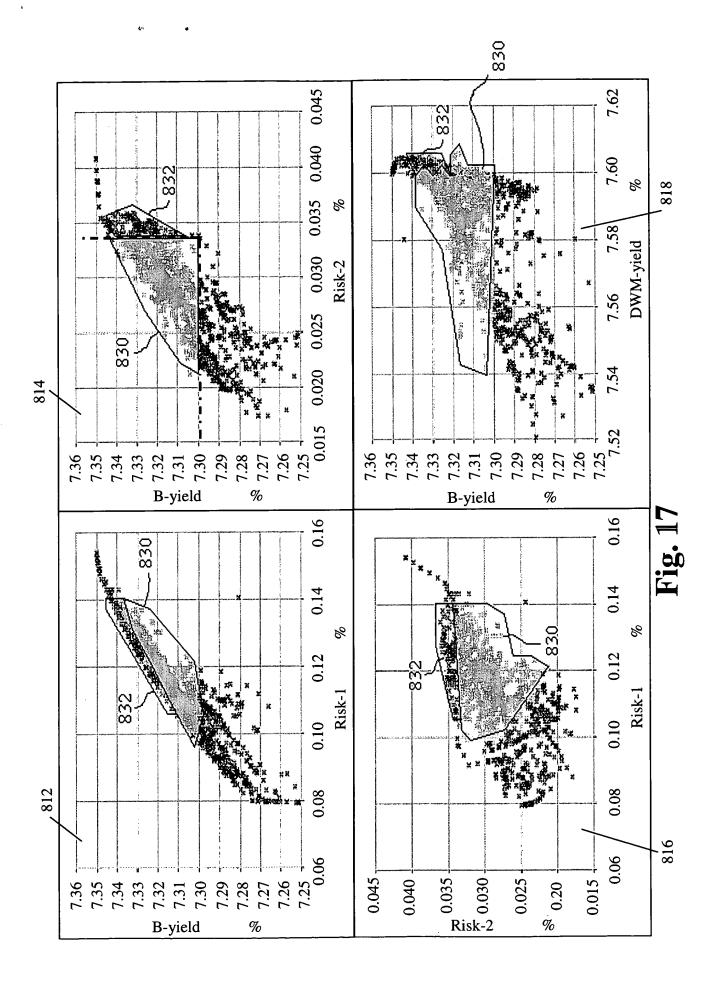
Muni Bonds Corporate Bonds Investment Type Equities Credit Risk 85 EXAMPLE OF PARALLEL COORDINATE PLOT **DWMYield Interest Risk** 25 1,500 5,000 3,000 5,550 250 VAR B Yield 50 Sigma

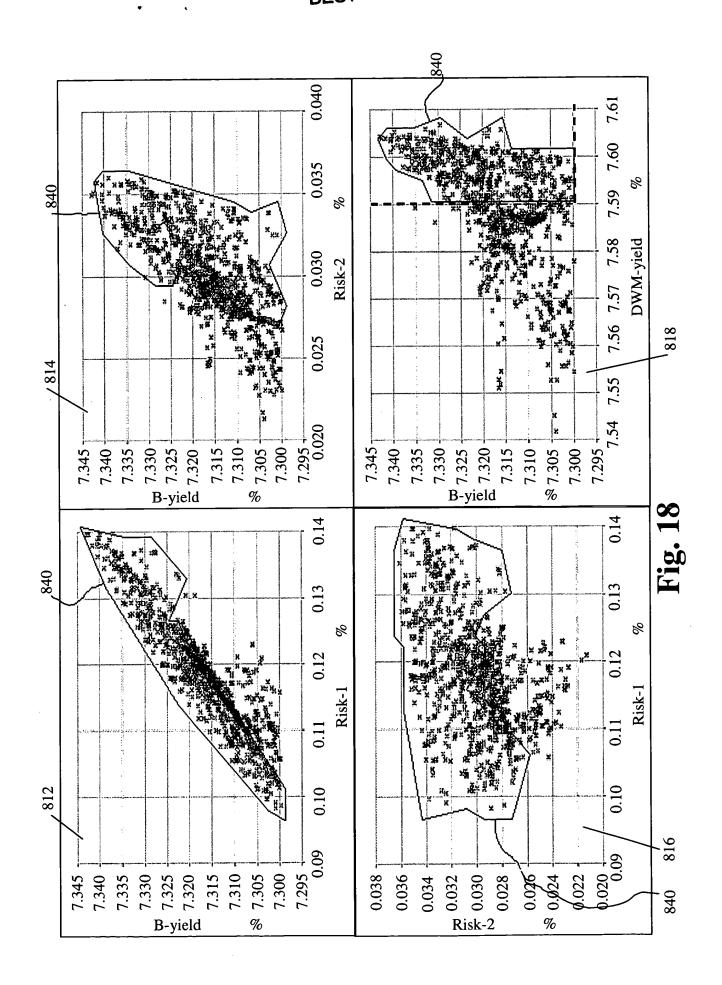
Fig. 14

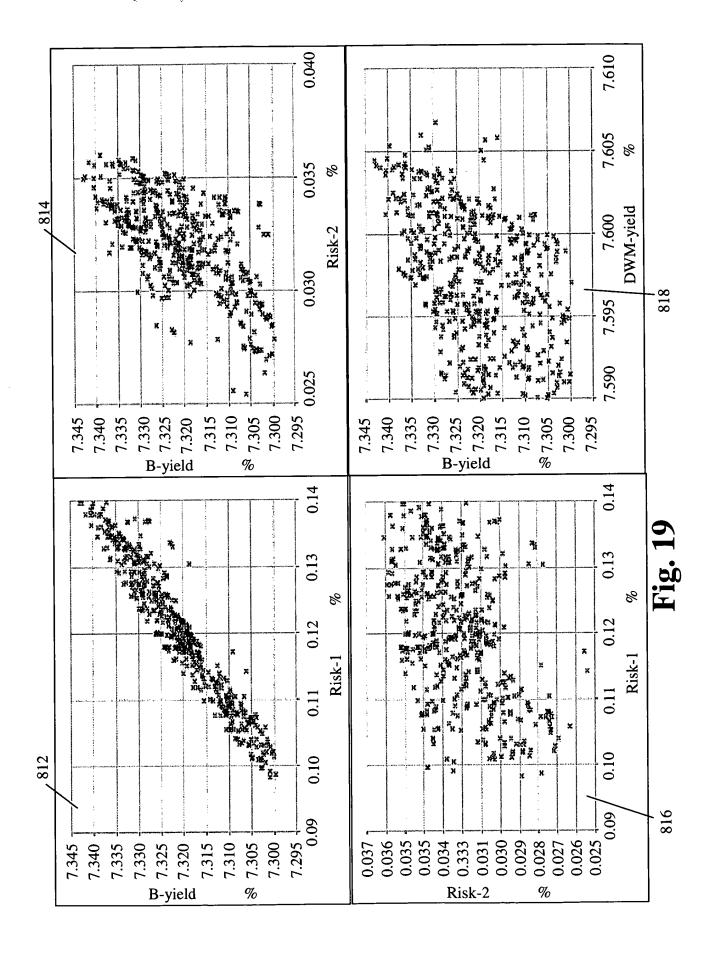


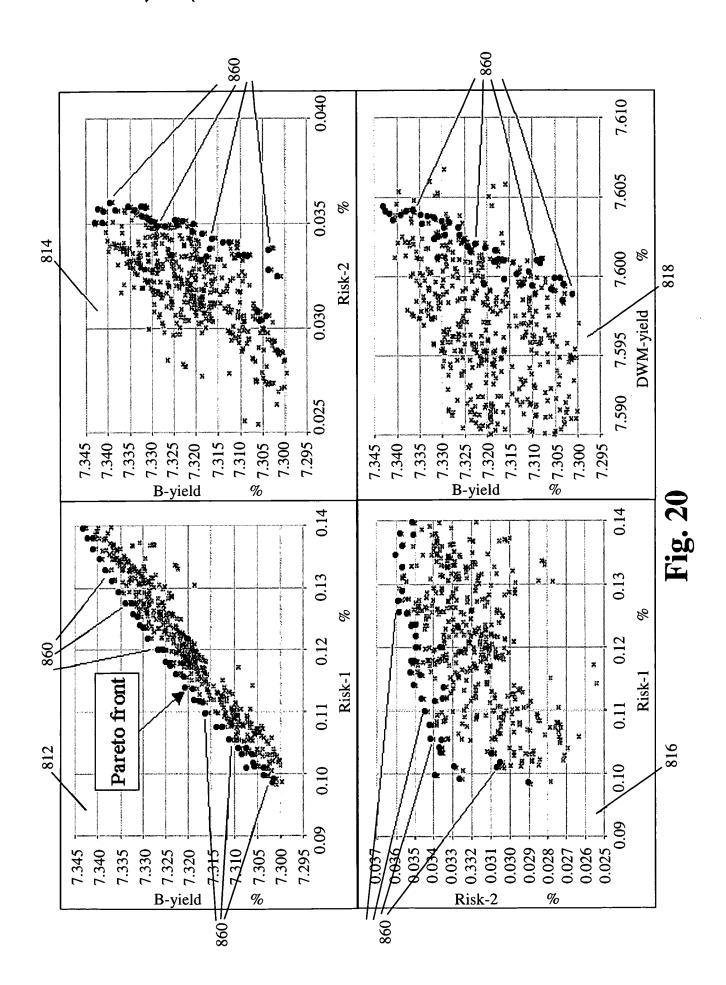
BEST AVAILABLE COPY

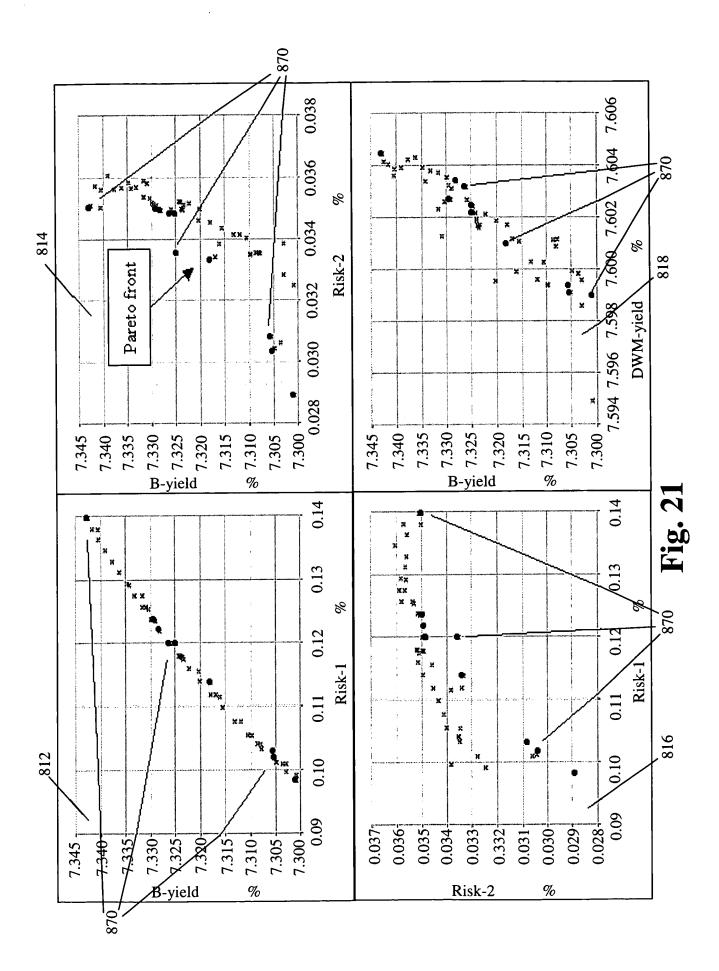


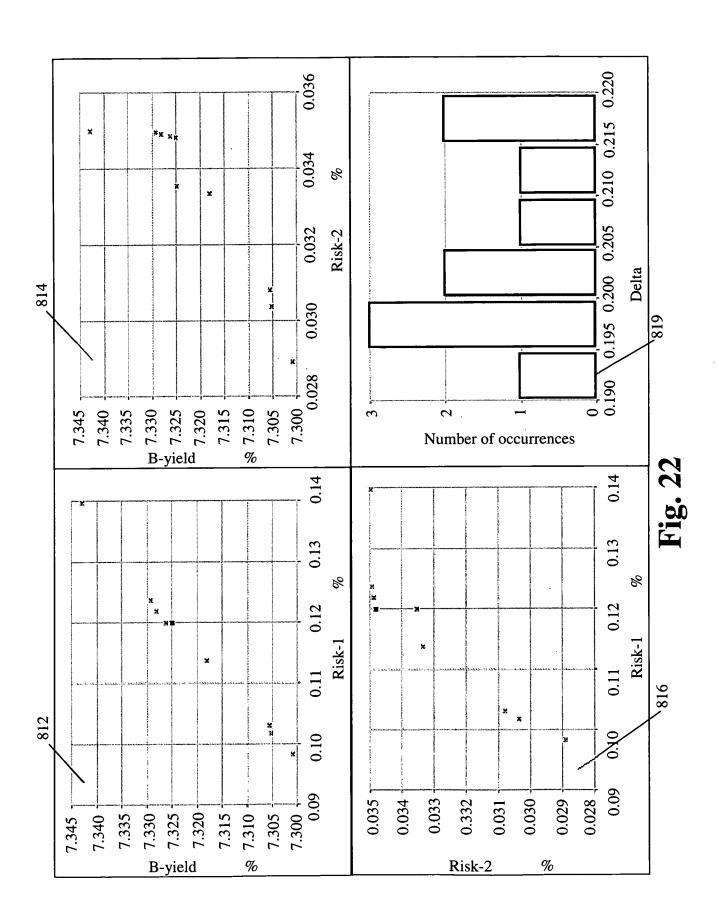












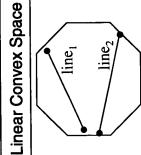
Feasible Regions for Optimization

Figure 33

GEAM

Graphic Visual

Word Description



- For any two points in the space, the line connecting the two points is always contained in the same space
- Space is defined using linear equations
- For any two points in the space, the line connecting the two points is always contained in the same

Nonlinear Convex

Space

spaceSpace is defined using some nonlinear equations

Nonlinear Nonconvex

Space

- For any two points in the space, the line connecting the two points is not always contained in the same space
- Space is defined using some nonlinear equations

Set of nonlinear equations

Example Equation $\begin{vmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \\ \vdots & \vdots \\ y \end{bmatrix} \le \begin{vmatrix} b_1 \\ b_2 \\ \vdots \\ \vdots \end{vmatrix}$

 Duration weighted yield formulation

 Market value weighted yield

formulation

Set of linear equations

 a_{82}

 a_{81}

$$\begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \\ \vdots & \vdots \\ a_{51} & a_{52} \end{bmatrix} \begin{bmatrix} x \\ y \\ \vdots \\ y \end{bmatrix} \le \begin{bmatrix} b_1 \\ b_2 \\ \vdots \\ b_5 \end{bmatrix}$$

Interest rate sigma

formulation

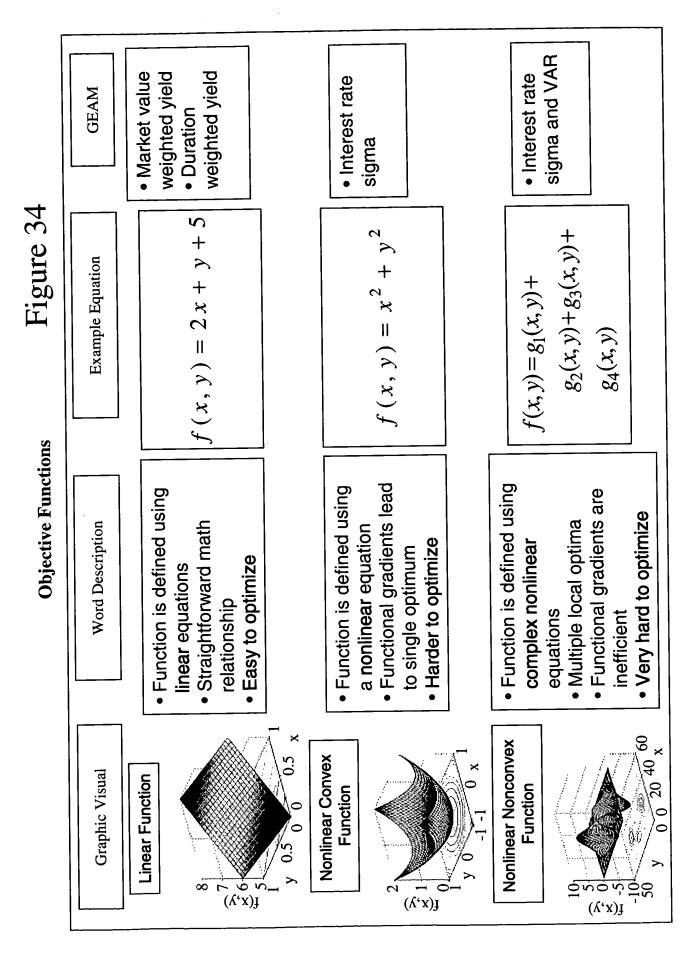
Nonlinear equation

8

VI

- VAR is a nonlinear nonconvex constraint

 a_{21} a_{22} a_{23}



Figure

Evolutionary Search Augmented with Domain Knowledge

Multi-objective portfolio optimization problem is formulated as a problem with Multiple linear, nonlinear and nonlinear nonconvex objectives. However, the domain knowledge allows us to use strictly linear and convex constraints.

Feasible Space

Feasible Space
Boundary
Points

P₂ O₂ O₁ P₂

Knowledge about geometry of feasible space (i.e. convexity), allowed us develop a feasible space boundary sampling algorithm (solutions archive generation). By knowing the boundary of the search space, we can exploit that knowledge to design efficient interior sampling methods.

Convex crossover is a powerful interior sampling method, which is guaranteed to produce feasible offspring solutions. Given parents P_1 , P_2 , it creates offspring $O_1 = \lambda P_1 + (1 - \lambda)P_2$, $O_2 = (1 - \lambda)P_1 + \lambda P_2$. An offspring O_k and P_k can crossed over to produce more diverse offspring.